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## INTRODUCTION TO LOGARITHMS Common Core Algebra II Homework

## FluENCY

1. Which of the following is equivalent to $y=\log _{7} x$ ?
(1) $y=x^{7}$
(3) $x=7^{y}$
(2) $x=y^{7}$
(4) $y=x^{1 / 7}$
2. If the graph of $y=6^{x}$ is reflected across the line $y=x$ then the resulting curve has an equation of
(1) $y=-6^{x}$
(3) $x=\log _{6} y$
(2) $y=\log _{6} x$
(4) $x=y^{6}$
3. The value of $\log _{5} 167$ is closest to which of the following? Hint - guess and check the answers.
(1) 2.67
(3) 4.58
(2) 1.98
(4) 3.18
4. Which of the following represents the $y$-intercept of the function $y=\log (x+1000)-8$ ?
(1) -8
(3) 3
(2) -5
(4) 5
5. Determine the value for each of the following logarithms. (Easy)
(a) $\log _{2} 32$
(b) $\log _{7} 49$
(c) $\log _{3} 6561$
(d) $\log _{4} 1024$
6. Determine the value for each of the following logarithms. (Medium)
(a) $\log _{2}(1 / 64)$
(b) $\log _{3}(1)$
(c) $\log _{5}(1 / 25)$
(d) $\log _{7}(1 / 343)$
7. Determine the value for each of the following logarithms. Each of these will have non-integer, fractional answers. (Difficult)
(a) $\log _{4} 2$
(b) $\log _{4} 8$
(c) $\log _{5} \sqrt[3]{5}$
(d) $\log _{2} \sqrt[5]{4}$
8. Between what two consecutive integers must the value of $\log _{4} 7342$ lie? Justify your answer.
9. Between what two consecutive integers must the value of $\log _{5}(1 / 500)$ lie? Justify your answer.

## APPLICATIONS

10. In chemistry, the pH of a solution is defined by the equation $\mathrm{pH}=-\log (H)$ where $H$ represents the concentration of hydrogen ions in the solution. Any solution with a pH less than 7 is considered acidic and any solution with a pH greater than 7 is considered basic. Fill in the table below. Round your pH 's to the nearest tenth of a unit.

| Substance | Concentration <br> of Hydrogen | $\mathbf{p H}$ | Basic or <br> Acidic? |
| :---: | :---: | :---: | :---: |
| Milk | $1.6 \times 10^{-7}$ |  |  |
| Coffee | $1.3 \times 10^{-5}$ |  |  |
| Bleach | $2.5 \times 10^{-13}$ |  |  |
| Lemon Juice | $7.9 \times 10^{-2}$ |  |  |
| Rain | $1.6 \times 10^{-6}$ |  |  |

## Reasoning

11. Can the value of $\log _{2}(-4)$ be found? What about the value of $\log _{2} 0$ ? Why or why not? What does this tell you about the domain of $\log _{b} x$ ?
